Internal quantum reference frames and external frame independence

In this talk, I will give an introduction to the internal quantum reference frame program and two broad ways of implementing an external frame independence via group averages. The choice depends on whether the given symmetry is a physical one or parametrizes a redundancy. This also leads to different notions of quantum reference frames that can peacefully co-exist within the same theory. I will illustrate this in lattice gauge theory.